

BACHELOR OF ARTS / SCIENCE WITH MATHEMATICS
4th SEMESTER
DISCIPLINE SPECIFIC COURSE (CORE-4)
(& GENERIC ELECTIVE COURSE FOR HONOURS PROGRAMMES)

MM420: MATHEMATICS: ALGEBRA

CREDITS: THEORY-4, TUTORIAL: 2

THEORY: MAXIMUM MARKS: 60, MINIMUM MARKS: 24

Objectives: The aim of this course is to learn the concepts of algebraic structures and their applications in other sciences.

UNIT-1 (15 HOURS)

Groups, Semi-groups and sub-groups, Cyclic groups and their sub-groups, cosets and Lagrange's theorem, product of sub-groups, counting principle for the number of elements in HK, normaliser and centre.

UNIT-2 (15 HOURS)

Normal subgroups and various criteria for normality of a sub-group, Quotient Groups, Group homomorphism and isomorphism, Examples.

UNIT-3 (15 HOURS)

Fundamental theorem of homomorphism, Correspondence theorem, second and third theorems of isomorphism, Permutation Group, Even and odd Permutations, Symmetric group of degree n, alternating group, simple group, Cayley's theorem.

UNIT-4 (15 HOURS)

Rings, Division rings and Fields, Sub-rings and Sub-fields, Ideals, Quotient rings, Principal ideals, Prime ideals, Maximal ideals and characterisations in terms of their associated quotient rings, Ring homomorphism and isomorphism, theorems on ring isomorphisms.

TUTORIALS (2 CREDITS: 30 HOURS) Maximum Marks: 30 Minimum Marks: 12

11. Tutorials based on Unit I & II - **1 credit**
12. Tutorials based on Unit III & IV – **1 credit**.

Books recommended

1. John B. Fraleigh, *A First Course in Abstract Algebra*, 7th Ed., Pearson 2002.
2. M. Artin, *Abstract Algebra*, 2nd Ed., Pearson 2011.
3. Joseph A Gallian, *Contemporary Abstract Algebra*, 4th Ed., Narosa 1999.
4. I. N. Herstein, *Topics in Algebra*.
5. S. Singh and Q. Zameer Din, *Modern Algebra*.