

## Semester - III

### Advanced Functional Analysis-- I

*Course No. MM-CP-304*  
*Duration of Examination: 3 hrs*

*Maximum Marks: 100*  
*(a) External Exam: 80*  
*(b) Internal Exam: 20*

#### **Unit I**

Complemented spaces Co not complemented in  $L_1$ . University of  $C[0,1]$  for separable Banach spaces, Banach-Alagolu theorem reflexive Banach spaces and their characterization terms of weak- compactness.

#### **Unit II**

Goldstine's theorem completeness and Dual of  $L_p [a,b], p$ . Extreme points, Krein-Milman theorem and its simple consequences,. Muntz theorem on  $C[a,b]$  and  $L_2 [a,b]$ .

#### **Unit III**

Topological vector spaces (TVS)" Definition and Examples. Basic properties –subspaces quotients and products of TVS. Bounded sets & totally bounded sets. Characterizing a linear topology in terms of local' base. Continuous and bounded linear maps between TVS.

#### **Unit IV**

Least upper bound and projective limits of linear topologies. Weak topology of a TVS Metrization and finite comensality in TVS. Completeness,, Sequential completeness and Quasi completeness in TVS and their relationship. E-Spaces and open mapping theorem/closed-graph theorem in F-spaces.

#### **References**

1. Ballobas, B;Lineart Analisis(Camb. Univ.Pres)
2. Goffman, C and Pedrick ,G; A first course in functional Analysis (Prentice Hall.)
3. Beauzamy, B;Indroduction to Banach Spaces and their geometry ( North Holland).
4. Wilansky, A: Modern Methods in topological Vector Spaces ( McGraw Hill).
5. Swatz C: Topological vector Spaces ( Marcel Dekker)
6. Rudin, W; Functional analysis ( Tata McGrawHill).
7. Jarchow ,H.,Locally Convex Spaces ( Teubner Texts).
8. Sachafer, H,H. topological Vector Spaces ( Springer Verlag).
9. Bachman, G & Narici, L., topological Vector spaces ( Marcel Dekker)